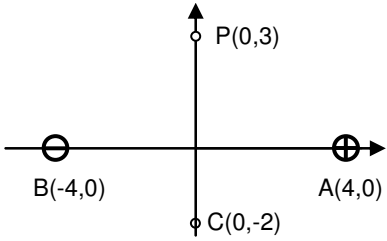




<p>1. Two point charges with magnitudes $+4\mu\text{C}$ and $-4\mu\text{C}$ are placed on points A and B, as can be seen on picture; lengths are given in m. Compute:</p> <p>a) Electric field on point P. b) Electric potential on point P. c) Work done to carry a $3\mu\text{C}$ point charge from point P to point (0,-2).</p> <p>2 points</p>	<p>1. Dos cargas puntuales de $+4\mu\text{C}$ y $-4\mu\text{C}$ se encuentran situadas en los puntos A y B respectivamente, tal como muestra la figura, con los valores expresados en metros. Calcula:</p> <p>a) El campo eléctrico en el punto P b) El potencial eléctrico en el punto P c) Trabajo realizado para llevar una carga de $3\mu\text{C}$ desde el punto P hasta el punto (0,-2).</p> <p>2 puntos</p>	
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<p>a) Electric field on point P will be due to both electric charges:</p> $E_p^+ = k \frac{4 \cdot 10^{-6}}{25} - 4\vec{i} + 3\vec{j} \quad E_p^- = k \frac{4 \cdot 10^{-6}}{25} - 4\vec{i} - 3\vec{j}$ <p>And the resulting electric field:</p> $\vec{E}_p = -2k \frac{4 \cdot 10^{-6}}{25} 4\vec{i} = -2,3 \cdot 10^3 \vec{i} \text{ V/m}$ <p>b) Electric potential on point P is zero, because both charges have the same magnitude (with different sign) and their distances to point P are equal: $V_p=0$.</p> <p>c) $W_{PC} = 3 \cdot 10^{-6} (V_p - V_C)$ Electric potential on point C is also zero $V_C=0$ (by the same reason that on point P). Then: $W_{PC} = 0 - 0 = 0$</p>	
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<p>2. State Gauss's law and apply it to compute the electric field produced by a sphere of radius R charged with surface density of charge σ:</p> <p>a) At a distance $2R$ from its center. b) At a distance $R/2$ from its center.</p> <p>2 points</p>	<p>2. Enuncia el teorema de Gauss y aplícalo para calcular el campo eléctrico creado por una esfera de radio R cargada con una densidad superficial de carga σ:</p> <p>c) A una distancia $2R$ de su centro d) A una distancia $R/2$ de su centro</p> <p>2 puntos</p>
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<p>Gauss's law: The flux of the electric field through a closed surface S equals the total charge enclosed inside such surface divided into the dielectric permittivity of vacuum.</p> <p>a) As surface S we choose a sphere with radius $2R$ concentric with the charged sphere. At any point of this surface, surface vector and electric field vector are parallel, and the magnitude of electric will also be constant. Then:</p> $\Phi = \oint_S \vec{E} \cdot d\vec{S} = \oint_S E \cdot dS = E \oint_S dS = E \cdot 4\pi(2R)^2 = \frac{\sigma 4\pi R^2}{\epsilon_0} \Rightarrow E = \frac{\sigma}{4\epsilon_0}$ <p>b) In this case, as inside a surface of radius $R/2$ we won't find any charge, electric flux and then electric field are zero.</p>	
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3. Picture shows 3 **equal** capacitors with capacitance **C** each, connected to a difference of potential **V₀**

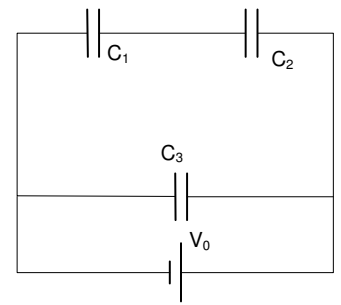
- Find the charge on each capacitor.
- The source is removed and a dielectric with relative dielectric permittivity $\epsilon_r=2$ is inserted between plates of capacitor **C₃**. Find the charge on each capacitor after inserting the dielectric.

2 points

3. La figura muestra 3 condensadores **iguales** de capacidad **C**, conectados a una diferencia de potencial **V₀**

- Halla la carga en cada condensador.
- Retiramos la fuente de tensión e introducimos un dieléctrico de permitividad relativa 2 en el condensador **C₃**. Halla la carga en cada condensador después de introducir el dieléctrico.

2 puntos



a) Capacitors 1 and 2 are connected in series, having equal charges: $Q_1=Q_2$.

The total difference of potential on both capacitors (1 and 2) equals the potential of source: $\frac{Q_1}{C} + \frac{Q_2}{C} = V_0$

Difference of potential on capacitor 3 is V_0 : $\frac{Q_3}{C} = V_0$

Solving this system of three equations with three unknowns, it becomes:

$$Q_1 = Q_2 = \frac{CV_0}{2} \quad \text{and} \quad Q_3 = CV_0$$

b) When source is disconnected and a dielectric is inserted inside capacitor 3, the new capacitance of such capacitor will be: $C'_3 = 2C$

Charge on capacitors 1 and 2, as they are connected in series, will be equal, but different to that of before point: $Q'_1=Q'_2$.

Total difference of potential on both capacitors (1 and 2) equals the potential on capacitor 3, being different than V_0 : $\frac{Q'_1}{C} + \frac{Q'_2}{C} = \frac{Q'_3}{2C}$

On the other hand, the total charge on capacitors 1 and 3 can't change before and after disconnecting the source, and then: $Q'_1+Q'_3 = Q_1+Q_3 = \frac{3}{2}CV_0$

Solving this system of three equations with three unknowns, it becomes:

$$Q'_1 = Q'_2 = \frac{3}{10}CV_0 \quad \text{and} \quad Q'_3 = \frac{6}{5}CV_0$$

4. Given the circuit on picture, compute:

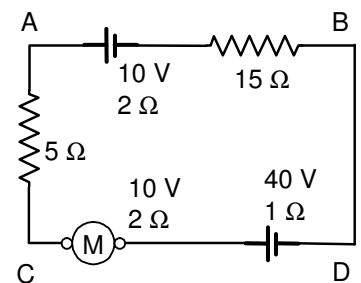
- Intensity of current flowing along the circuit (magnitude and sense).
- Difference of potential between points **A** and **B** (**V_{AB}**)
- Supplied power by the 40 V generator.
- Consumed power by the engine.

2 points

4. Dado el circuito de la figura, calcula:

- Intensidad que circula por el circuito (valor y sentido)
- Diferencia de potencial entre **A** y **B** (**V_{AB}**)
- Potencia suministrada por el generador de 40 V.
- Potencia consumida por el motor.

2 puntos



a) Assuming the intensity flows in clockwise sense:

$$I = \frac{40 - 10 - 10}{1 + 2 + 5 + 2 + 15} = \frac{20}{25} = 0,8 \text{ A} \quad \text{As result is positive, the assumed sense for intensity is correct.}$$

b) $V_{AB} = 0,8(2 + 15) - (-10) = 23,6 \text{ V}$

c) $P_s = \mathcal{E}I - I^2r = 40 \cdot 0,8 - 0,8^2 \cdot 1 = 31,36 \text{ w}$

d) $P_c = \mathcal{E}'I + I^2r' = 10 \cdot 0,8 + 0,8^2 \cdot 2 = 9,28 \text{ w}$

5. Given the circuit on picture, compute:

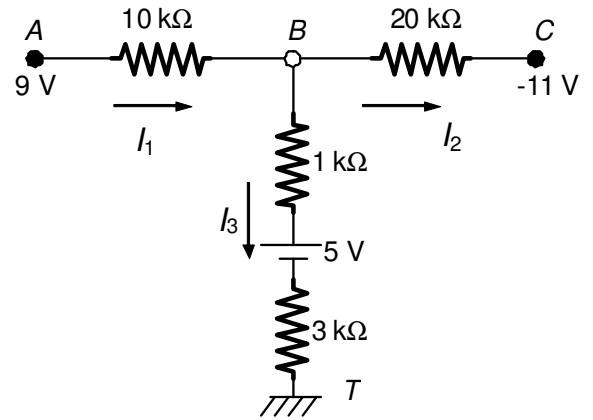
- The intensity of current flowing along each branch.
- The equivalent resistance of circuit between A and B.
- Thevenin's equivalent generator between A and B and the intensity of current that would flow along a 5 kΩ resistor connected between A and B.

2 points

5. Dado el circuito de la figura, calcula:

- La intensidad que circula por cada una de las ramas.
- La resistencia equivalente entre A y B.
- El generador equivalente de Thevenin entre A y B, y la intensidad de corriente que circularía por una resistencia de 5 kΩ que conectásemos entre A y B.

2 puntos



a) Applying Kirchhoff's rules:

Rule of junctions: $\Sigma I = 0$
 $I_1 = I_2 + I_3$

Rule of loops: $V_A - V_T = 9 = 10I_1 + 4I_3 + 5$
 $V_C - V_T = -11 = -20I_2 + 4I_3 + 5$

Solving this system:

$$I_1 = 0,5 \text{ mA} \quad I_2 = 0,75 \text{ mA} \quad I_3 = -0,25 \text{ mA}$$

b) Equivalent resistance between A and B:

On circuit can be seen that resistors of 1 and 3 KΩ are connected in series, and their equivalent resistor is connected in parallel with 20 and 10 KΩ resistors. Then:

$$\frac{1}{4} + \frac{1}{20} + \frac{1}{10} = \frac{1}{R_{eq}}; \quad R_{eq} = 2,5 \text{ K}\Omega$$

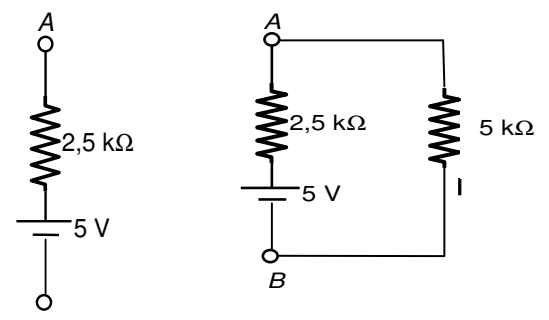
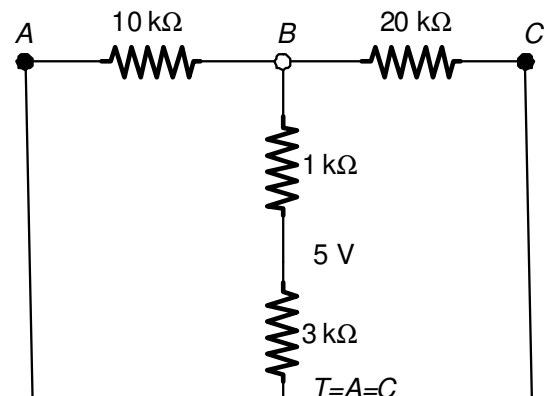
c) Thèvenin's equivalent generator between A and B:

$$\varepsilon_T = V_A - V_B = 10 \cdot 0,5 = 5 \text{ V}$$

$$R_{eq} = 2,5 \text{ K}\Omega$$

If a 5KΩ resistor is connected between A and B, intensity flowing this resistor is:

$$I = \frac{\Sigma \varepsilon}{\Sigma R} = \frac{5}{2,5 + 5} = 0,66 \text{ mA}$$



FORM

Electrostatics

$$\vec{F} = K \frac{q_1 q_2}{r^2} \vec{u}_r \quad \vec{E} = \frac{\vec{F}}{q} \quad K = \frac{1}{4\pi\epsilon_0} = 9 \cdot 10^9 \text{ (S.I.)} \quad V_A - V_B = \int_A^B \vec{E} \cdot d\vec{r}$$

$$\vec{E} = K \frac{q}{r^2} \vec{u}_r \quad V = K \frac{q}{r} \quad \int_S \vec{E} \cdot d\vec{S} = \frac{\sum Q}{\epsilon_0} \quad W_{AB} = q(V_A - V_B)$$

Conductors and capacitors

$$E = \frac{\sigma}{\epsilon_0} \quad C = \frac{Q}{V} \quad C = \frac{\epsilon_0 S}{d}$$

$$C_{eq} = \sum C_i \quad \frac{1}{C_{eq}} = \sum \frac{1}{C_i} \quad E_d = \frac{E}{\epsilon_r} \quad C_d = \epsilon_r C \quad W = \frac{Q^2}{2C} = \frac{QV}{2} = \frac{V^2 C}{2}$$

Direct Current

$$\vec{J} = n \cdot e \cdot \vec{v}_a \quad \vec{J} = \sigma \cdot \vec{E} \quad R = \frac{V_1 - V_2}{I} \quad R = \rho \frac{L}{S}$$

$$\rho = \rho_0 (1 + \alpha(T - T_0)) \quad V_A - V_B = I \sum R - \sum \epsilon \quad I = \frac{\sum \epsilon}{\sum R} \quad P = V \cdot I$$

$$\epsilon = \frac{dW}{dq} \quad P_R = R \cdot I^2 \quad P_g = \epsilon \cdot I \quad P_t = \epsilon' \cdot I \quad P_g - P_r = P_s \quad P_t + P_r = P_c$$

$$\eta_g = \frac{P_s}{P_g}$$

$$\eta_r = \frac{P_t}{P_c}$$