



1. Three equal point charges $+q$ are resting and placed as can be seen on picture, at a distance a from point O. Compute:

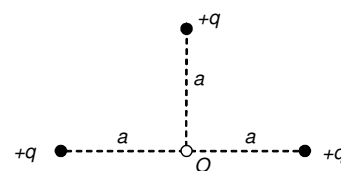
- a) The total electric force that such charges will produce on a charge q' placed on O.
b) The electrostatic potential energy having q' on O.

2 points

1. Tres cargas puntuales iguales de valor $+q$ se encuentran en reposo, situadas como se ve en la figura, a una distancia a del punto O. Calcula:

- a) la fuerza eléctrica total que las cargas producirán sobre una carga q' situada en O.
b) La energía potencial electrostática de q' en O.

2 puntos



a) The force produced on q' by those charges located on horizontal axis are cancelled, and then the only force acting on q' is due to the upper charge: $F_{q'} = k \frac{q \cdot q'}{a^2}$ N pointing to down if q' is positive.

b) The electric potential produced on O by the charges is: $V_o = 3k \frac{q}{a}$ V

And the electrostatic potential energy of q' on O: $U_{q'} = q' V_o = q' 3k \frac{q}{a} = \frac{3kq q'}{a}$ J

2. From a conductor material having resistivity ρ , two cylindrical wires with the same length L are built, but with different radii R and $2R$ each. Both wires are connected in series, and a voltage V is applied to this set. Compute the intensity of current flowing along each wire.

1,5 points

2. De un material conductor de resistividad ρ se fabrican dos cables cilíndricos de la misma longitud L , pero de radios R y $2R$ cada uno de ellos. Se conectan en serie, y al conjunto se le aplica una tensión V . Calcular la corriente que circula por cada uno de los cables.

1,5 puntos

Resistances of both wires are: $R_a = \rho \frac{L}{\pi R^2} \Omega$ and $R_{2a} = \rho \frac{L}{\pi (2R)^2} = \rho \frac{L}{4\pi R^2} \Omega$

When both wires are connected in series, the total resistance is $R = R_a + R_{2a} = \frac{\rho L}{\pi R^2} (1 + \frac{1}{4}) = \frac{5\rho L}{4\pi R^2} \Omega$

And the intensity of current is the same for both wires: $I = I_a = I_{2a} = \frac{V}{R} = \frac{4V\pi R^2}{5\rho L}$ A

3. Between points A and B of shown set of capacitors, a difference of potential V is applied. Three capacitors are equal, with capacitance C . Find:

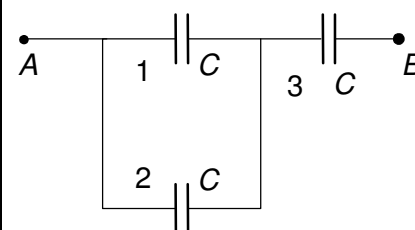
- a) Charge on each capacitor.
b) Difference of potential between terminals of each capacitor.
c) Stored energy on capacitor 2. Results must be given as a function of C and V .

2 points

3. Entre los puntos A y B de la asociación de condensadores de la figura se aplica una diferencia de potencial V . Los tres condensadores son iguales, de capacidad C . Halla:

- a) La carga en cada condensador.
b) La diferencia de potencial entre los bornes de cada condensador.
c) La energía almacenada en el condensador 2. Los resultados deben darse en función de C y V .

2 puntos



a) If Q_1, Q_2 and Q_3 and V_1, V_2 and V_3 are the charge and potential on each capacitor is verified that:

About charges: $Q_1=Q_2$ $Q_1+Q_2= Q_3$

About potentials: $V_1=V_2$ $V_1+V_3=V$ or $V_2+V_3=V$

From charges: $2Q_1 = Q_3 \Rightarrow Q_1 = \frac{Q_3}{2}$ and replacing on equation of potentials taking in account that

$$C = \frac{Q_1}{V_1} = \frac{Q_2}{V_2} = \frac{Q_3}{V_3} : \quad \frac{Q_3}{2} + \frac{Q_3}{C} = V \Rightarrow Q_3 = \frac{2}{3}CV \quad \text{and} \quad Q_1 = Q_2 = \frac{1}{3}CV$$

b) $V_1 = V_2 = \frac{1}{3}V$ and $V_3 = \frac{2}{3}V$

a) can also be solved using the idea of equivalent capacitance:

Equivalent capacitance of 1 and 2 (they are in parallel) is $C_{12} = C + C = 2C$ This equivalent capacitor

is in series with 3, being their equivalent capacitance $\frac{1}{C_{123}} = \frac{1}{C_{12}} + \frac{1}{C} = \frac{1}{2C} + \frac{1}{C} = \frac{3}{2C} \Rightarrow C_{123} = \frac{2}{3}C$

The charge taken by the equivalent capacitor is $Q_{123} = C_{123}V = \frac{2}{3}CV$

$$Q_3 = Q_{123} = \frac{2}{3}CV \quad \text{and} \quad Q_1 = Q_2 = \frac{1}{2}Q_3 = \frac{1}{3}CV$$

c) Stored energy on 2 is: $W_2 = \frac{Q_2^2}{2C} = \frac{C^2V^2}{9 \cdot 2C} = \frac{1}{18}CV^2$

4. On circuit on picture, compute:

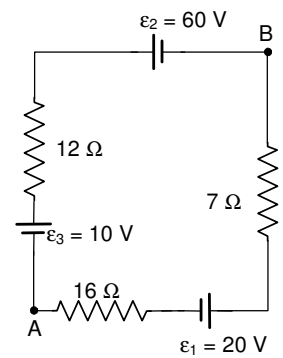
- Intensity of current flowing along circuit.
- Difference of potential between points A and B.
- Clearly state which devices on circuit are acting as generators and which are acting as receptors.
- Consumed power on 7Ω resistor and generated power on ϵ_1 .

2 points

4. En el circuito de la figura, calcula:

- La intensidad de corriente del circuito.
- La diferencia de potencial entre los puntos A y B.
- Indica claramente qué elementos actúan como generadores y cuáles como receptores.
- La potencia disipada en la resistencia de 7Ω , y la potencia generada por ϵ_1 .

2 puntos



a) Assuming intensity flows in counterclockwise sense:

$$I = \frac{\sum_i \epsilon_i}{\sum_j R_j} = \frac{60 - 10 + 20}{12 + 16 + 7} = \frac{70}{35} = 2 \text{ A}$$

b) $I = V_A - V_B = I \sum_{AB} R_j - \sum_{AB} \epsilon_i = 2(16 + 7) - 20 = 26 \text{ V}$

c) Generators (intensity flows from negative to positive terminal inside the device): ϵ_1 and ϵ_2

Receptors: ϵ_3

d) $P_R = I^2 R = 2^2 \cdot 7 = 28 \text{ w}$

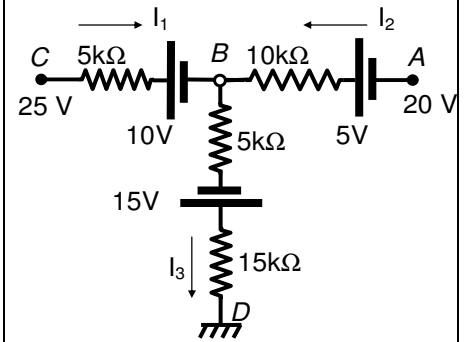
$P_{\epsilon_1} = 20 \cdot 2 = 40 \text{ w}$

5. On circuit on picture, compute:
 a) Intensity of current flowing along each branch of circuit, with the shown senses.
 b) Difference of potential between points A and B.
 c) Equivalent resistance of passive circuit between points A and B.
 d) Drawn the equivalent Thevenin's generator between points A and B, clearly showing its polarity.

2,5 points

5. Dado el circuito de la figura:
 a) Calcula la intensidad que circula por cada rama, con los sentidos indicados.
 b) Calcula la diferencia de potencial entre A y B.
 c) Calcula la resistencia equivalente del circuito pasivo entre A y B.
 d) Representa, indicando la polaridad, el generador equivalente de Thevenin entre A y B.

2,5 puntos

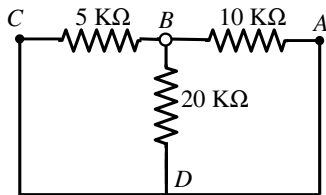


a) This is a network with 2 junctions and two loops, and so we'll need one equation for junctions and two equations for loops:

$$\left. \begin{aligned} I_1 + I_2 &= I_3 \\ V_{CD} = 25 &= I_1 \cdot 5 - (-10) + I_3(15 + 5) - (15) \\ V_{AD} = 20 &= I_2 \cdot 10 - (5) + I_3(15 + 5) - (15) \end{aligned} \right\} \Rightarrow I_1 = \frac{2}{7} \text{ mA} \quad I_2 = \frac{8}{7} \text{ mA} \quad I_3 = \frac{10}{7} \text{ mA}$$

b) $V_A - V_B = 10I_2 - (5) = \frac{45}{7} \text{ V}$

c) Passive circuit and equivalent resistance between A and B (removing all the generators) is:



Between A and B, three resistors are in parallel: $\frac{1}{R_{eqAB}} = \frac{1}{5} + \frac{1}{10} + \frac{1}{20} \Rightarrow R_{eqAB} = \frac{20}{7} \text{ K}\Omega$

d) So, Thevenin's equivalent generator between A and B is:

