

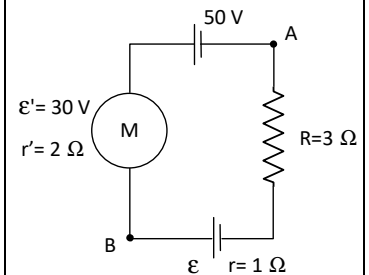


1. (2,5 points) On circuit on picture, the **ideal generator** with electromotive force **50 V** is acting as a generator, and the **internal resistance of the other generator consumes** a power of **4 w**.

- State the **polarity** of receptor M.
- Compute the **intensity** flowing along the circuit.
- Compute the unknown **electromotive force ϵ** .
- Compute the **difference of potential** between points **A and B**.
- Compute the **generated powers** and the **consumed powers** on circuit, doing a balance of power.
- Compute the **efficiency** of receptor M.

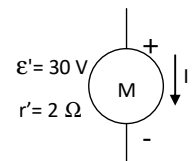
1. (2,5 puntos) En el circuito de la figura, el **generador ideal** de f.e.m. **50 V** está actuando como generador, y la **resistencia interna del otro generador consume** una potencia de **4 w**.

- Indica la **polaridad** del receptor M.
- Calcula la **intensidad** que recorre el circuito.
- Calcula la **fuerza electromotriz** desconocida ϵ .
- Calcula la **diferencia de potencial** entre los puntos **A y B** del circuito.
- Haz un balance de potencias, calculando las **potencias generadas** y las **consumidas** en el circuito.
- Calcula el **rendimiento** del receptor M.



Solution:

- If it's said that the 50 V generator acts as a generator, then the intensity must flow on the circuit in counterclockwise direction. So, as the intensity must enter on a receptor through the positive terminal, the upper terminal of motor is the positive terminal, and the lower terminal, the negative one.
- As the power consumed on the internal resistor of ϵ ($r=1 \Omega$) is 4 w: $4 = I^2 \cdot 1 \Rightarrow I = 2 \text{ A}$
- From the equation of circuit: $2 = \frac{50 - 30 - \epsilon}{2 + 1 + 3} \Rightarrow \epsilon = 50 - 30 - 12 = 8 \text{ V}$
- The difference of potential can be calculated by going from A to B through two different paths:
 - Through receptor: $V_A - V_B = 2 \cdot 2 - (50 - 30) = 4 - 20 = -16 \text{ V}$
 - Through generator ϵ : $V_A - V_B = -2 \cdot 4 - (8) = -16 \text{ V}$
 Obviously, in both cases the result is the same.



- The only generated power is that of 50 V generator: $P_g = \mathcal{E}I = 50 \cdot 2 = 100 \text{ w}$

The consumed powers are:

- On receptor: $P_c = \mathcal{E}' \cdot I + I^2 r' = 30 \cdot 2 + 4 \cdot 2 = 68 \text{ w}$
- On generator ϵ : $P_c = \mathcal{E} \cdot I + I^2 r = 8 \cdot 2 + 2^2 \cdot 1 = 20 \text{ w}$
- On resistor: $P_R = I^2 R = 4 \cdot 3 = 12 \text{ w}$

Obviously, the generated power equals the consumed powers: $100 = 68 + 20 + 12$.

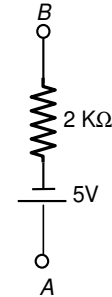
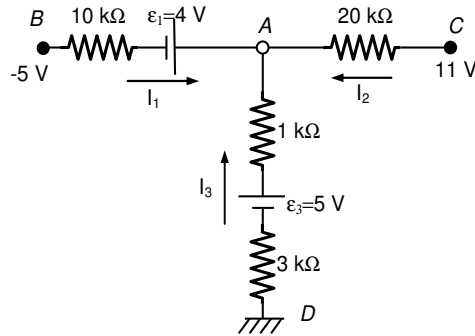
- $\eta' = \frac{P_t}{P_c} = \frac{30 \cdot 2}{68} = 0,88 = 88 \%$

2. (3 points) Given the circuit on picture, compute:

- Intensity of current flowing along each branch with the shown directions, I_1 , I_2 and I_3 .
- Thevenin's equivalent generator between points A and B, clearly showing its polarity.
- If the branch on right is connected between points A and B, say if the 5 V generator of the new branch is acting as a generator or as a receptor.
- Thevenin's equivalent generator between points B and D, clearly showing its polarity.

2. (3 puntos) Dado el circuito de la figura, calcula:

- La intensidad de corriente en cada rama con los sentidos mostrados, I_1 , I_2 y I_3 .
- El generador equivalente de Thevenin entre los puntos A y B, indicando claramente su polaridad.
- Si la rama de la derecha se conecta entre los puntos A y B, di si el generador de 5 V de la nueva rama actúa como generador o como receptor.
- El generador equivalente de Thevenin entre los puntos B y D, indicando claramente su polaridad.

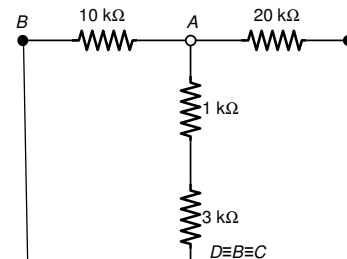


Solution:

This is a network with 2 junctions and two loops, and so we'll need one equation for junctions and two equations for loops:

$$\left. \begin{aligned} I_1 + I_2 + I_3 &= 0 \\ V_{BD} = -5 &= 10I_1 - 4 - 4I_3 - (-5) \\ V_{CD} = 11 &= 20I_2 - 4I_3 - (-5) \end{aligned} \right\} \Rightarrow I_1 = -\frac{21}{40} = -0,525 \text{ mA} \quad I_2 = \frac{27}{80} = 0,337 \text{ mA} \quad I_3 = \frac{3}{16} = 0,187 \text{ mA}$$

$$b) \quad \mathcal{E}_T = V_{AB} = V_A - V_B = -10I_1 - (-4) = \frac{37}{4} = 9,25 \text{ V}$$

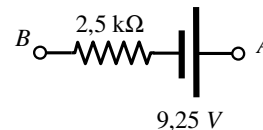


Passive circuit after removing all the generators is

and its equivalent resistance between A and B is:

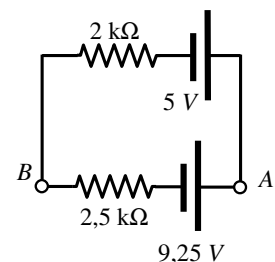
$$\frac{1}{R_{eqAB}} = \frac{1}{10} + \frac{1}{4} + \frac{1}{20} \Rightarrow R_{eqAB} = \frac{5}{2} = 2,5 \text{ k}\Omega$$

So, Thevenin's equivalent generator between A and B is:

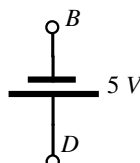


- If we connect the new branch between points A and B, the resulting circuit is:

In this circuit, the intensity flows in counterclockwise direction, and then, the 5 V generator is acting as a receptor.



- $\mathcal{E}_T = V_{BD} = -5 \text{ V} \quad R_{eqBD} = 0$

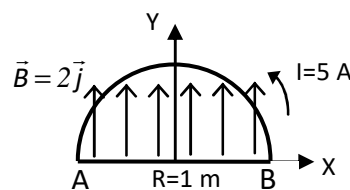


3. (2 points) A **loop** is made up by a **semicircumference** and a **straight conductor** connecting both endings of semircumference (A and B), as can be seen on picture. The radius of the loop is $R=1\text{ m}$, and it's flowed by an intensity of current $I=5\text{ A}$. A **uniform magnetic field** $\vec{B}=2\vec{j}$ is acting on the loop.

- Compute the **force** acting over the **rectilinear** part of the loop, between A and B, giving the **result as a vector**.
- Write the magnetic moment of the loop, $\vec{\mu}$, writing it as a **vector**.
- Compute the torque $\vec{\tau}$ acting on the loop.
- Compute the **force** acting over the **semicumference**, between A and B, giving the **result as a vector**.

3. (2 puntos) Una **espira** está formada por una **semicircunferencia** y por un **conductor rectilíneo** que une ambos extremos de la semicircunferencia (A y B), como puede verse en la figura. El radio de la espira es $R=1\text{ m}$, y está recorrida por una corriente $I=5\text{ A}$. Un **campo magnético uniforme** $\vec{B}=2\vec{j}$ actúa sobre la espira.

- Calcula la **fuerza** que actúa sobre la parte **rectilínea** de la espira, entre A y B, dando el resultado en **forma vectorial**.
- Escribe el momento magnético de la espira, $\vec{\mu}$, dando el resultado en **forma vectorial**.
- Calcula el momento $\vec{\tau}$ que actúa sobre la espira.
- Calcula la **fuerza** que actúa sobre la **semicunferencia**, entre A and B, dando el resultado en **forma vectorial**.



Solution:

- $\vec{F}_1 = I\vec{\ell} \times \vec{B} = 5 \cdot 2\vec{i} \times 2\vec{j} = 20\vec{k}\text{ N}$
- $\vec{\mu} = I\vec{S} = I \cdot \frac{\pi R^2}{2} \vec{k} = \frac{5\pi}{2} \vec{k}\text{ Am}^2$
- $\vec{\tau} = \vec{\mu} \times \vec{B} = \frac{5\pi}{2} \vec{k} \times 2\vec{j} = -5\pi \vec{i}\text{ Nm}$
- As the total force acting over the loop must be null, then the force acting over the semicumference is opposite to that acting over the rectilinear conductor: $\vec{F}_2 = -20\vec{k}\text{ N}$

4. (2,5 points) Two infinite straight carrying current conductors, with a distance d between them, are placed on plane **XY**. They are carrying currents $I_1=2I$ and $I_2=I$ in **opposite directions**. Compute the **magnetic field** created by both currents at points:

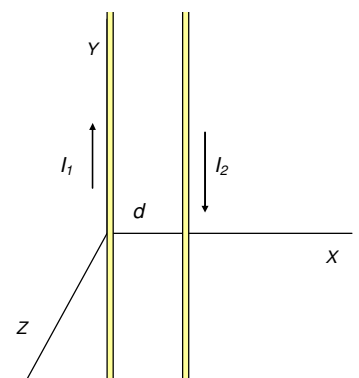
- A ($d/2, 0, 0$).
- B ($2d, 0, 0$).
- C ($0, 0, d$).

On each case, give the result as a **vector**.

4. (2,5 puntos) Dos conductores rectilíneos e indefinidos, separados una distancia d , están situados en el plano **XY**, y llevan sendas corrientes $I_1=2I$ y $I_2=I$ en **sentidos contrarios**. Calcula el **campo magnético** creado por ambas corrientes en los puntos:

- A ($d/2, 0, 0$).
- B ($2d, 0, 0$).
- C ($0, 0, d$).

En cada caso, expresa el **resultado como un vector**.



Solution:

On every case, the magnetic field is the summatory of magnetic fields produced by each conductor:

$$a) \vec{B}_A = \vec{B}_1 + \vec{B}_2 = -\frac{\mu_0 2I}{2\pi \frac{d}{2}} \vec{k} - \frac{\mu_0 I}{2\pi \frac{d}{2}} \vec{k} = -\frac{3\mu_0 I}{\pi d} \vec{k}$$

$$\text{b) } \vec{B}_B = \vec{B}_1 + \vec{B}_2 = -\frac{\mu_0 2I}{2\pi 2d} \vec{k} + \frac{\mu_0 I}{2\pi d} \vec{k} = 0$$

$$\text{c) } \vec{B}_C = \vec{B}_1 + \vec{B}_2 = \frac{\mu_0 2I}{2\pi d} \vec{i} + \frac{\mu_0 I}{2\pi d \sqrt{2}} \frac{-\vec{i} - \vec{k}}{\sqrt{2}} = \frac{\mu_0 I}{\pi d} \vec{i} + \frac{\mu_0 I}{4\pi d} (-\vec{i} - \vec{k}) = \frac{\mu_0 I}{\pi d} \vec{i} - \frac{\mu_0 I}{4\pi d} \vec{i} - \frac{\mu_0 I}{4\pi d} \vec{k} = \frac{\mu_0 I}{4\pi d} (3\vec{i} - \vec{k})$$

FORM

Direct current $V_A - V_B = I \sum R - \sum \mathcal{E}$ $I = \frac{\sum \mathcal{E}}{\sum R}$ $P = V \cdot I$ $\mathcal{E} = \frac{dW}{dq}$ $P_R = I^2 \cdot R$

$P_g = \mathcal{E} \cdot I$ $P_t = \mathcal{E}' \cdot I$ $P_g - P_r = P_s$ $P_t + P_r = P_c$ $\eta_g = \frac{P_s}{P_g}$ $\eta_r = \frac{P_t}{P_c}$

Magnetic Forces $\vec{F} = q(\vec{v} \times \vec{B})$ $d\vec{F} = Id\vec{l} \times \vec{B}$ $\vec{\mu} = N \cdot I \cdot \vec{S}$ $\vec{\tau} = \vec{\mu} \times \vec{B}$ $V_H = \frac{I \cdot B \cdot d}{n \cdot e \cdot S}$

Sources of magnetic field $d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{\ell} \times \vec{r}}{r^3}$ $\mu_0 = 4\pi 10^{-7} \text{ (I.S. units)}$ $B = \frac{\mu_0 I}{2\pi x}$

$B = \frac{\mu_0 I}{2R}$ $\oint_L \vec{B} \cdot d\vec{l} = \mu_0 \sum I$ $B = \frac{\mu_0 NI}{l}$